

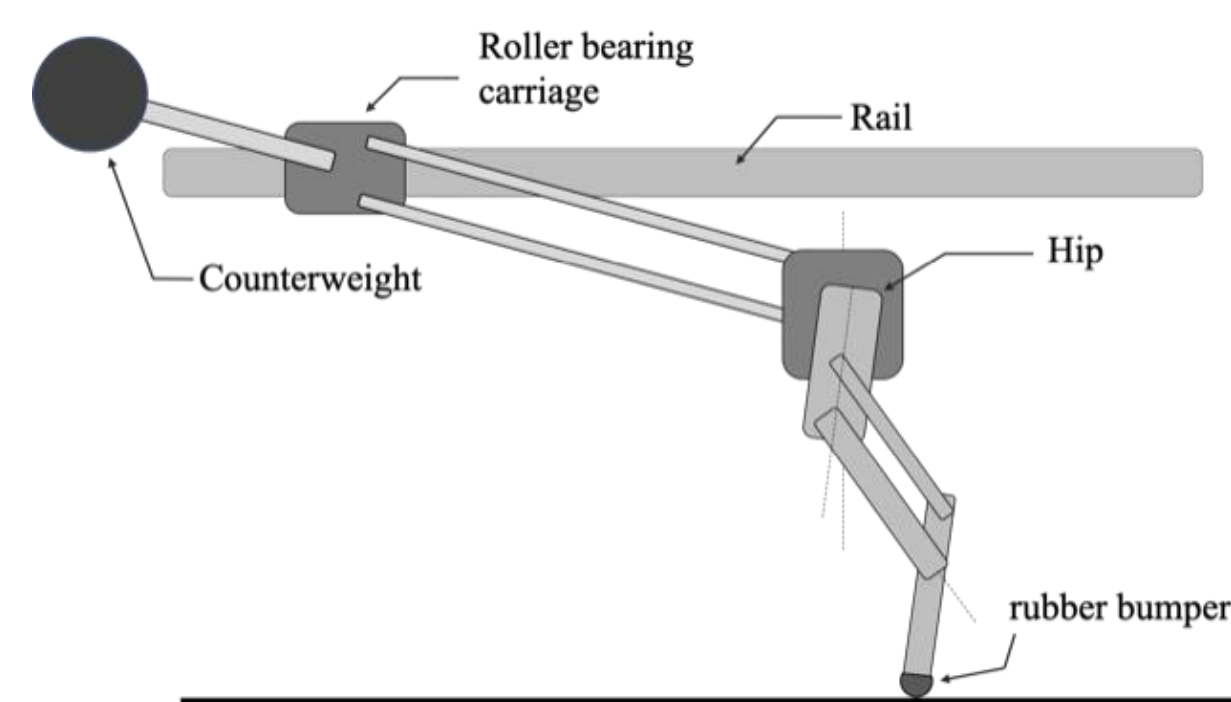
# The Effect of Variable Jumping Frequency on Cost of Transport

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## Introduction

- For legged locomotion, moving at constant velocity can be achieved with two types of strides or jumps
  - Case 1: Frequent, short distance
  - Case 2: Infrequent, long distance
- Examples: Kangaroos, human walking vs. running
- Which type of motion is more energy efficient?

**Objective Question:** How does cost of transport (CoT) differ between longer jumps and shorter jumps?



## Control Strategy

Time-based, phase-dependent control

- Torque control for  $0 < t < t_{stance}$
- Impedance Control in Task Space for  $t_{stance} < t \leq t_{jump}$
- Reset time to 0 when  $t > t_{jump}$

\*\* Does not require contact detection

## Data Analysis

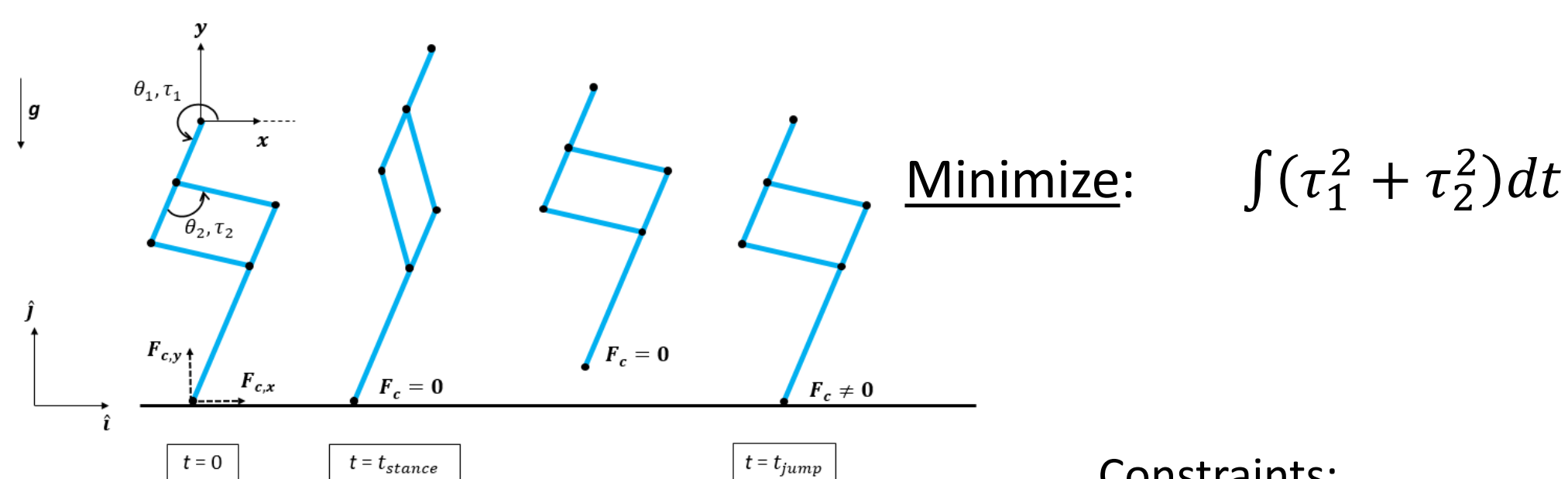
For a single jump:

$$E_{total} = \underbrace{\int R(I_1^2 + I_2^2)dt}_{\text{Joule Heating}} + \underbrace{\int \tau_1 d\theta_1 + \tau_2 d\theta_2}_{\text{Work done by system}}$$

$$P_{avg} = \frac{E_{total}}{t_{jump}}$$

$$CoT = \frac{P_{avg}}{MgV}$$

## Simulation Methods



**Degrees of freedom:**  $x, y, \theta_1, \theta_2$

**Control inputs:**  $\tau_1, \tau_2$

**Other generalized forces:**  $F_{x,c}, F_{y,c}$

**No hyperextension:**  $0 \leq \theta_2 \leq \pi$

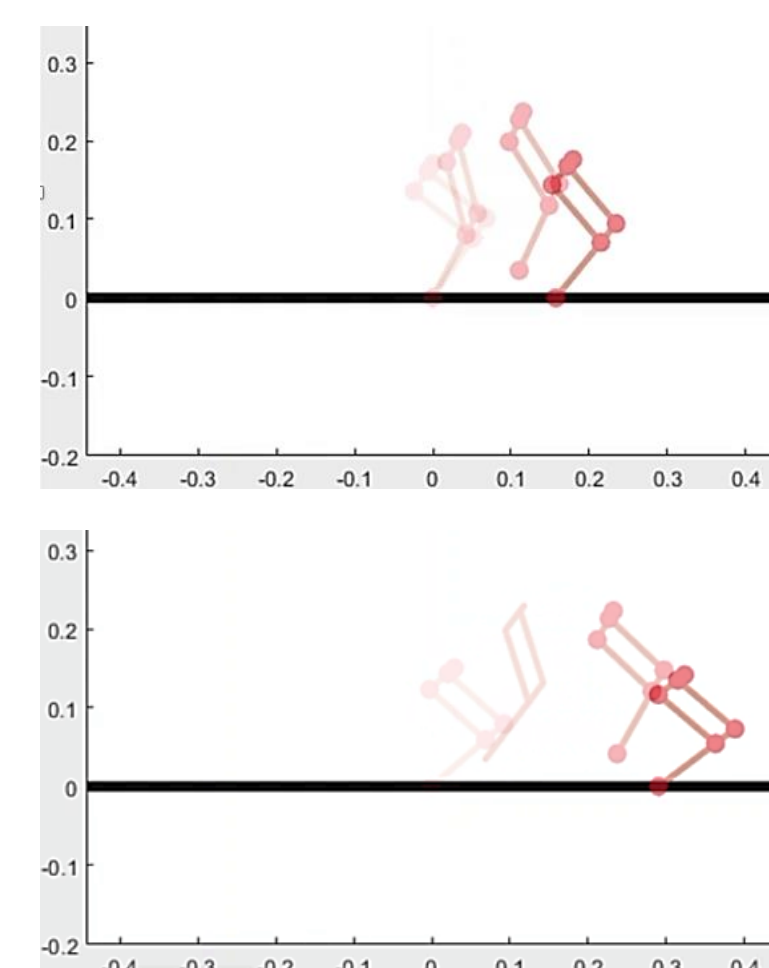
**No slip:**  $|F_{c,x}| \leq \mu |F_{c,y}|$

**Constant speed:**  $\frac{x_{end}}{t_{jump}} = V_{desired}$

Jump is cyclical

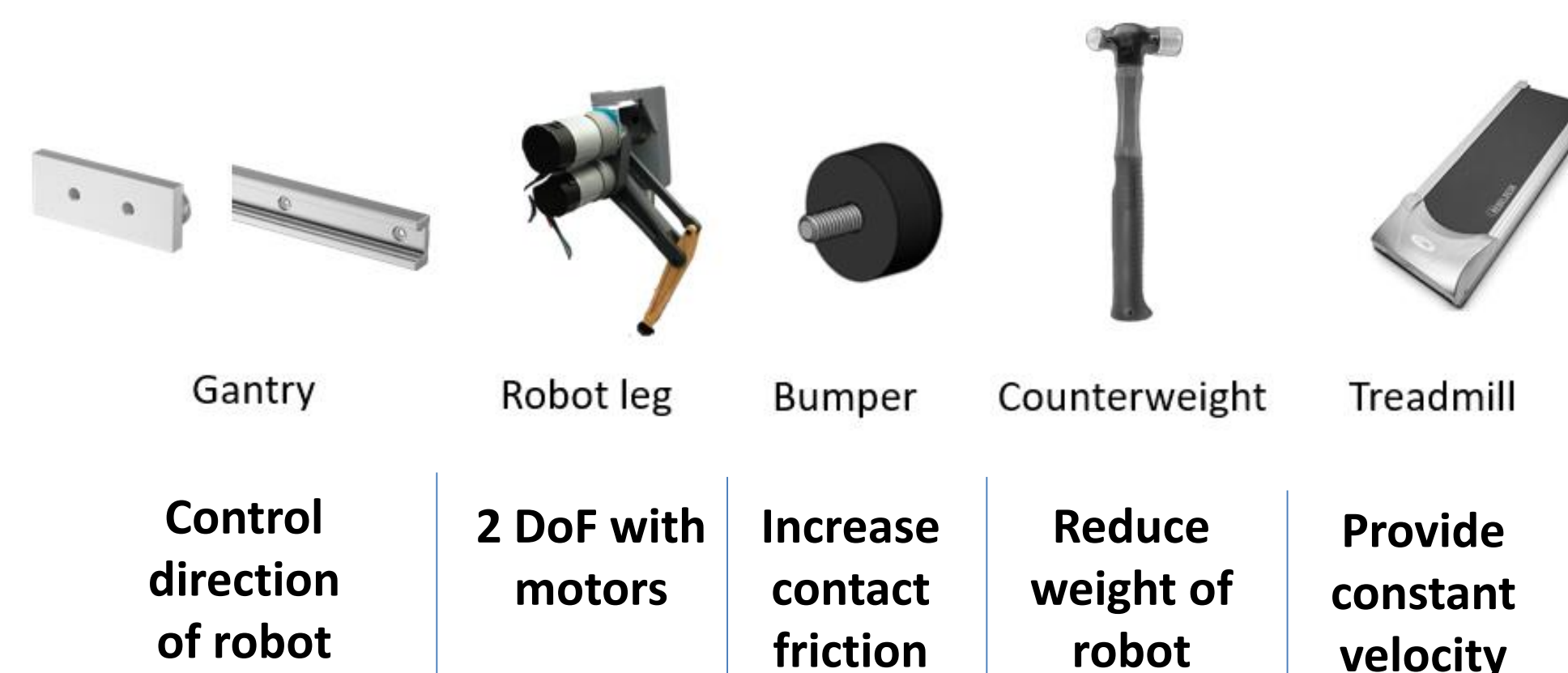
## Simulation Results

Case	Time between jumps (sec)	Cost of Transport
1	0.38	28.3
2	0.62	28.9



Cost of transport is similar between high frequency and low frequency

## Experimental Methods



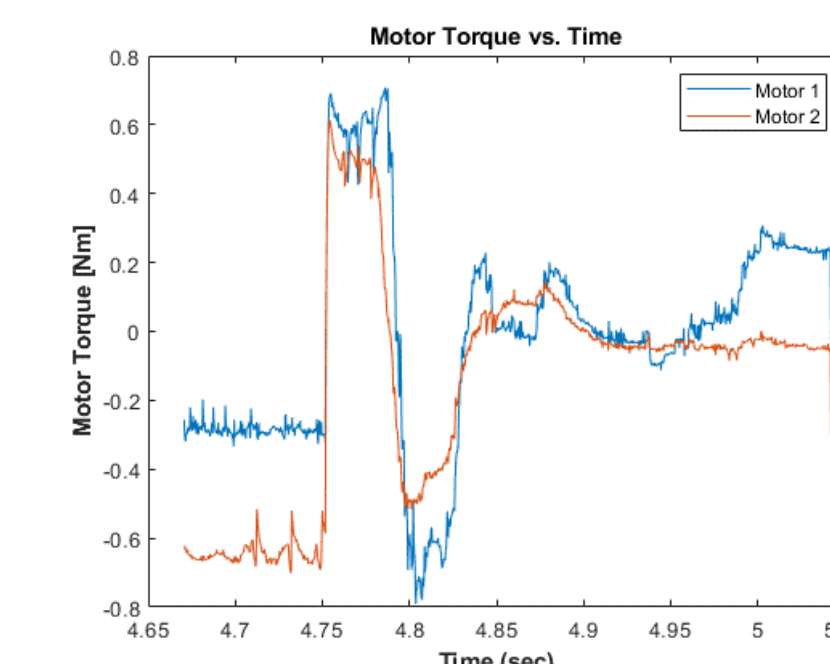
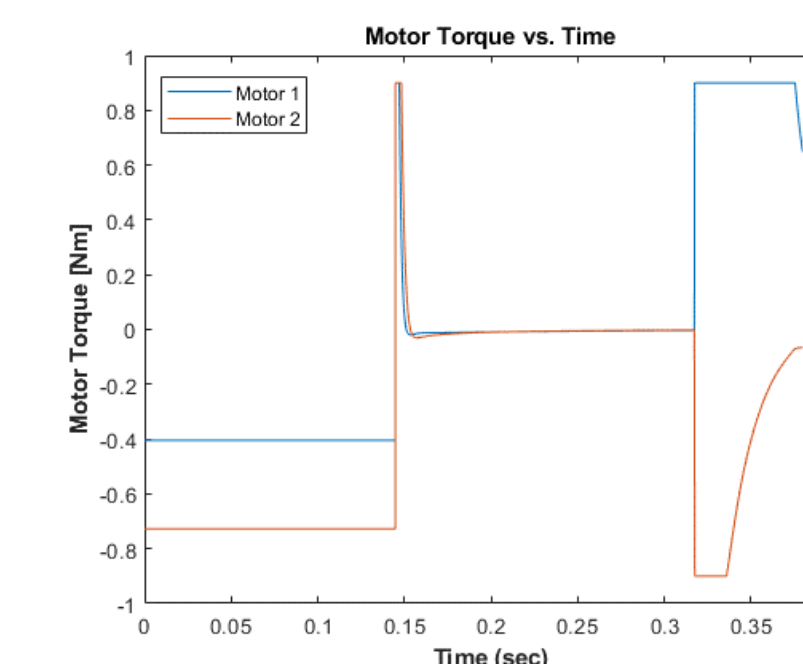
## Experimental Results

Case	Time between jumps (sec)	Cost of Transport
1	0.38	23.2 ± 1.5
2	0.63	40.8 ± 1.2

Cost of transport is lower for high frequency jumping

## Discussion

- Control scheme behaves as predicted by simulation
- CoT values are similar between simulation and hardware
- Knee motor consistently saturated to allow robot to jump
- Foot slipping was occasionally observed (could solve with improved contact friction)
- Some out-of-plane motion was observed; should stiffen hardware for future tests



## Conclusion

- From simulation, we predicted that the CoT would be similar between high and low frequency jumping
- From experiments, CoT was significantly lower for high frequency jumping

## References

[1] S Seok, Sangbae Kim, Design Principles for Energy-Efficient Legged Locomotion and Implementation on the MIT Cheetah Robot, Transactions on Mechatronics